

# المختبر الثاني

## Exercice 1

$$1. P_r = \frac{P}{P_c} \quad P_c = \sum x_i P_{c,i} = 0,7 P_{c,1} + 0,3 P_{c,2}$$

$$P_{c,1} = 4,26 \text{ MPa} \Rightarrow P_c = 4,122 \text{ MPa} \quad (0,25)$$

$$P_{c,2} = 3,8 \text{ MPa}$$

$$T_r = \frac{T}{T_c} \quad T_c = \sum x_i T_{c,i} = 0,7 T_{c,1} + 0,3 T_{c,2}$$

$$T_{c,1} = 370 \text{ K} \Rightarrow T_c = 386,56 \text{ K} \quad (0,25)$$

$$T_{c,2} = 425,2 \text{ K}$$

$$\Rightarrow P_r = \frac{10,3}{4,122} = 2,50 \quad T_r = \frac{250 + 173,1 \cdot 1,35}{386,56} \quad (0,25)$$

## 2. Specific volume

a. for ideal case:  $PV = nRT \Rightarrow P v_d = \frac{RT}{M}$

$$v_d = \frac{RT}{PM} \Rightarrow v_d = \frac{8,314 \times (250 + 173,1)}{10,3 \cdot 10^6 \cdot 48,2}$$

$$M = 0,7 \times 44 + 0,3 \cdot 58 = 48,2 \text{ g/mol} \quad (0,25)$$

$$v_d = 8,76 \cdot 10^{-6} \text{ m}^3/\text{g} \quad (0,25) \quad v_d = 8,76 \cdot 10^{-3} \text{ m}^3/\text{kg}$$

b. for real behaviour:  $P v_r = Z \frac{RT}{M} \quad (0,25)$

$$\Rightarrow v_r = \frac{Z \cdot RT}{PM} = Z v_d$$

from chart:  $Z(2,50, 1,35) \approx 0,685$

$$\approx 0,69 \quad (0,25)$$

8

$$\rightarrow \rho_{\text{nat}} = 0,69 \cdot 8,76 \cdot 10^3 = 6,04 \cdot 10^3 \text{ m}^3/\text{kg} \quad \text{Cor}$$

Exercise 2  $V_m = 90x_1 + 180x_2 + x_1x_2(15x_1 + 5x_2)$

$$x_1 = 1 - x_2 \quad \text{Cor}$$

$$\rightarrow V_m = 180 - 25x_1 + 5x_1^2 + 10x_1x_2 \quad \text{Cor}$$

1.  $V_1^* = 90 \text{ cm}^3/\text{mol}$   $V_2^* = 180 \text{ cm}^3/\text{mol}$  Cor

2.  $V_{\text{ideal}} = 90x_1 + 180x_2$  Cor

3.  $\bar{V}_1 = V_m + (1-x_1) \frac{dV_m}{dx_1}$  Cor  $\bar{V}_2 = V_m - x_1 \frac{dV_m}{dx_1}$

$$\frac{dV_m}{dx_1} = -25 + 10x_1 - 20x_1^2 \quad \text{Cor}$$

$$\bar{V}_1 = 95 + 10x_1 - 35x_1^2 + 20x_1^3 \quad \text{Cor}$$

$$\bar{V}_2 = 180 - 5x_1^2 + 20x_1^3 \quad \text{Cor}$$

4.  $x_2 = 0,3$   $x_1 = 0,7$

$$\left. \begin{aligned} V_m &= 101,52 \text{ cm}^3/\text{mol} \quad \text{Cor} \\ \bar{V}_1 &= 91,77 \text{ cm}^3/\text{mol} \quad \text{Cor} \\ \bar{V}_2 &= 124,41 \text{ cm}^3/\text{mol} \quad \text{Cor} \\ V^E &= 101,52 - 99 = 2,52 \text{ cm}^3/\text{mol} \quad \text{Cor} \end{aligned} \right\} 0,25 \quad \text{Cor}$$

Exercise 3

1. The diagram represents solid-liquid E of non-ideal mixture binary with partially miscible components 0,75

1, 2

- 1 - Pb rich solution
- 2 - solid - liquid equilibrium (Pb rich)
- 2' - " " " " (Sn-rich)
- 3 - Liquid solution
- 4 - solid - solid Mixture (~~Pb-Sn~~)  
(Pb rich + Sn-rich)  
(solid solid)

3.  $T_A \approx 325^\circ\text{C}$        $T_B = 230^\circ\text{C}$       (air)

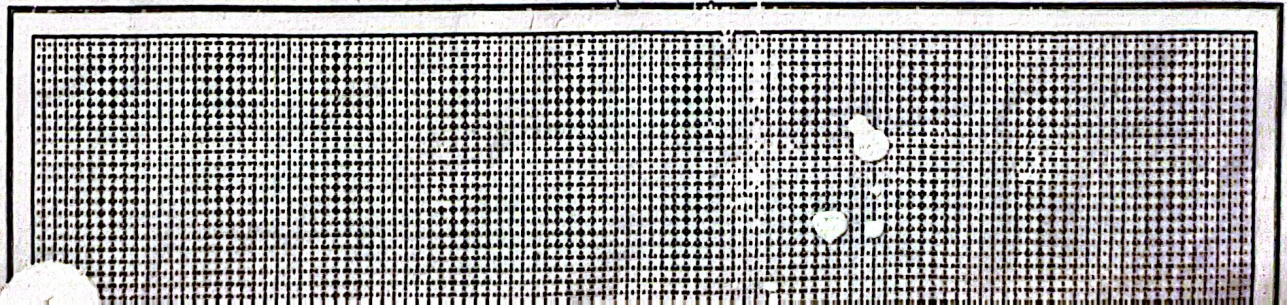
4. E. Eutectic Point ( $\approx 62\%$ ,  $183^\circ\text{C}$ )  
(air)

The composition of the mixture at E:

- 3 Phase Phases:
- } Pb rich solid
  - } Sn rich solid (air)
  - } Liquid Pb + Sn

Main Properties:

- } as Pure Matter
- } melt / solidify at constant  $T$
- } Liquid composition =  $x_{\text{mixt}}$  (air)



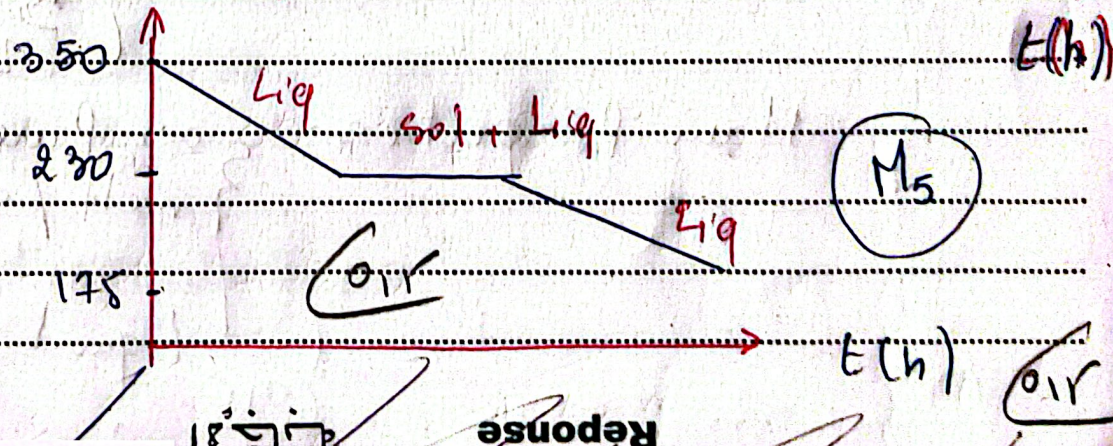
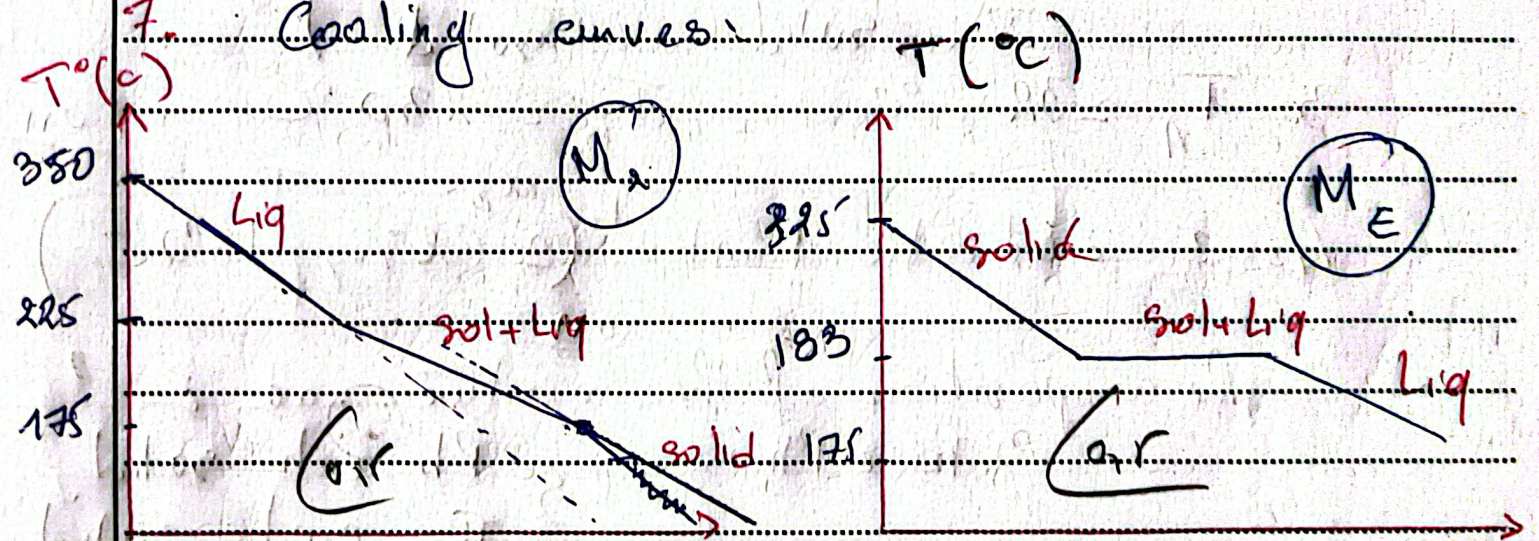
5. Table

6. for  $M_2$  (40% B, 225)

first drop: 19% Pb-rich solid (OIR)

first solid: 13% Sn, 87% Pb (OIR)

7. Cooling curves



Response

$$x_A = 65\% \quad , \quad T = 225$$

$$81 \quad n_T = 15 \text{ mole}$$

$$\begin{cases} n_{sol} + n_{liq} = 15 \\ n_{sol} = \frac{46 - 35}{35 - 17} = \frac{11}{18} = 0.61 \end{cases} \quad \text{Cor}$$

$$n_{sol} = 0.61 n_{liq}$$

$$\rightarrow n_{liq} + 0.61 n_{liq} = 15$$

$$n_{liq} = 9.32 \text{ mol} \quad n_{sol} = 5.68 \text{ mol} \quad \text{Cor}$$

$$n_{liq} \begin{cases} 0.17 \times 9.32 = 1.58 \text{ mol of B} \\ x_A = 7.74 \text{ mol of A} \end{cases}$$

$$* \quad x_A = 65\% \quad T = 125^\circ C$$

$$x_B = 35\%$$

$$n_T = 15 \text{ mol} \Rightarrow n_{solid A} + n_{solid B} = 15$$

$$\text{using Lever Rule: } \frac{n_{solid A}}{n_{solid B}} = \frac{x_{liq} - x_m}{x_m - x_{solid}} = \frac{97 - 35}{35 - 8} = \frac{62}{27} = 2.3 \quad \text{Cor}$$

$$\begin{cases} n_{solid A} = 2.3 n_{solid B} \Rightarrow n_{solid B} + 2.3 n_{solid B} = 15 \end{cases}$$

$$\Rightarrow n_{solid B} = \text{Cor}$$

$$\text{we have } x_{solid A} = 8\% \quad \text{and} \quad x_{solid B} = 97\% \quad \text{Cor}$$

$$n_{solid A} \begin{cases} n^B = \\ n^A = \end{cases}$$

$$n_{solid B} \begin{cases} n^B = \\ n^A = \end{cases}$$

0,25

0,15

0,25

0,25

0,4

Mixture	$M_1$	$M_2$	$M_3$	$M_4$	$M_5$
position of mixture	10% B 90% A	35% B 65% A	70% B 30% A	85% B 15% A	100% B 0% A
existing Phases	A-rich solid	Solid-Liquid	Liquid	Solid A + solid B	Liquid
composition of phase I	10% B 90% A	Solid: 17% B 83% A	70% B 30% A	A-rich sol	100% B
composition of phase II	/	Liquid: 47% B 53% A	/	B-rich sol	/
temperature of melting	275 °C	182° - 250°	180° - 190°	182° - 217° ≈	≈ 230°C

1,25

