

Unit Operations II Final Exam

Closed Notes, Show All Work

Exercise 1: (Graded out of 12 points)

In an industrial refrigeration plant, as shown in **Figure 1**, a forced-draft cooling tower (**Figure 2**) is used to cool condenser water. Atmospheric air enters the base of the tower and is forced upward through the falling water spray by a centrifugal fan. The cooled water collects in a basin at the bottom.

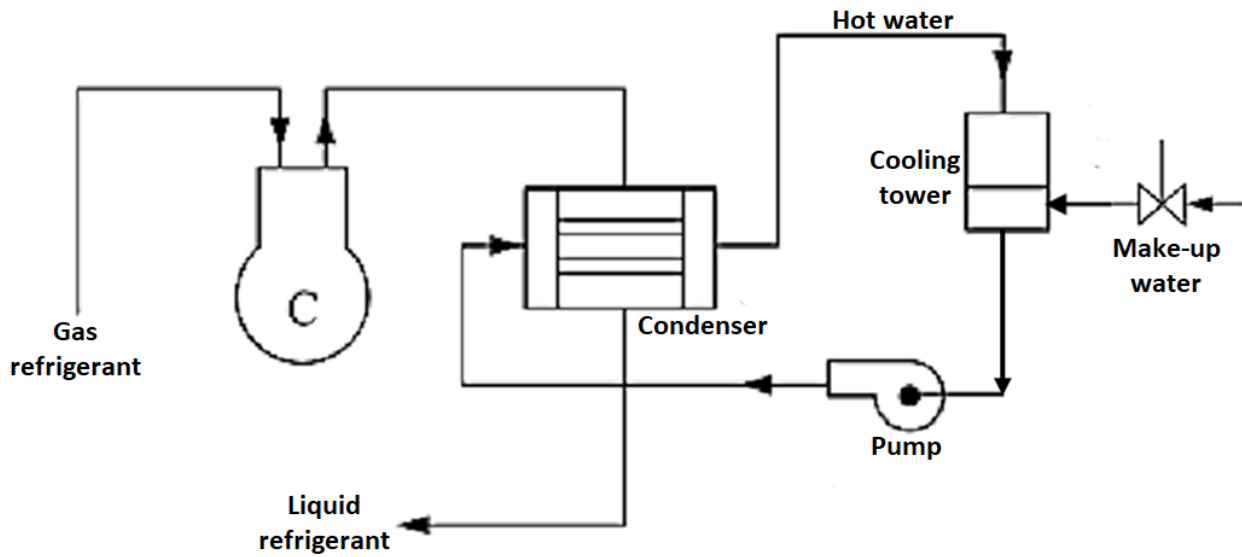


Figure 1 – an industrial refrigeration plant.

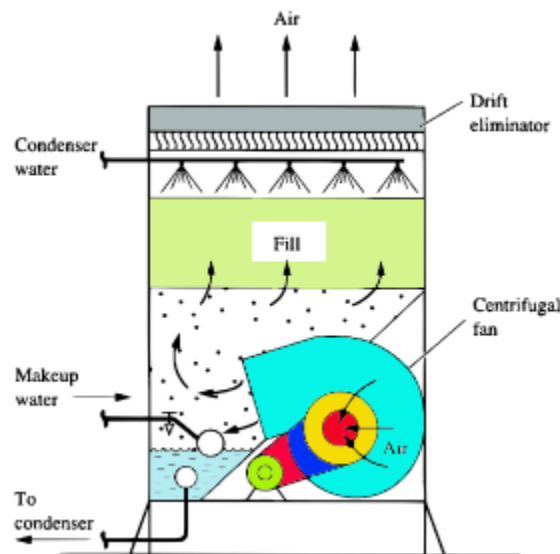


Figure 2 – a forced-draft cooling tower.

The following operating conditions have been recorded during a performance test.

Given data:

Water circuit		Air circuit	
Hot water inlet temperature	$T_{w,in} = 40\text{ °C}$	Inlet dry-bulb temperature	$T_{DB,1} = 35\text{ °C}$
Approach temperature	$\Delta T_{app} = 3\text{ °C}$	Inlet wet-bulb temperature	$T_{WB,1} = 28\text{ °C}$
Mass flow rate of water	$\dot{m}_w = 5\ 000\text{ kg/min}$	Outlet dry-bulb temperature	$T_{DB,2} = 38\text{ °C}$
Specific heat of water	$c_{p,w} = 4.187\text{ kJ/(kg}\cdot\text{K)}$	Outlet relative humidity	$\phi_2 = 60\%$

QUESTIONS —

PART A — PSYCHROMETRIC CHART READING (COMPLETE BEFORE ANY CALCULATION)

Using a standard psychrometric chart at $P = 101.325\text{ kPa}$, locate both air states and read off the following properties. Record your readings in the table — these values will feed directly into Parts B and C.

Property	Symbol	State 1 — air inlet 35 °C DB · 28 °C WB	State 2 — air outlet 38 °C DB · 60% RH
Specific enthalpy	h (kJ/kg d.a.)
Humidity ratio	ω (kg/kg d.a.)
Wet-bulb temperature (outlet only)	$T_{WB,2}$ (°C)	/
Dew-point temperature	T_{DP} (°C)

PART B — WATER-SIDE ANALYSIS

- 1) Determine the cold water outlet temperature, $T_{w,out}$.
- 2) Calculate the total heat rejected by water stream, Q_w .

PART C — ENERGY BALANCE AND AIR FLOW

- 1) Give the steady-state energy balance for the tower.
- 2) Calculate the required dry-air flow rate, \dot{m}_a , through the cooling tower in: **kg dry air.min⁻¹**.
- 3) Determine the amount of make-up water, $\dot{m}_{make-up}$, required to compensate for evaporative losses, Express your answer as a percentage of the inlet water flow.

PART D — DISCUSSION

- 1) On your psychrometric chart, sketch and label the process path of the air (State 1 → State 2). Describe the simultaneous heat and mass transfer processes occurring as air rises through the tower.
- 2) If the inlet air relative humidity increased from its current value to **80%** (at the same dry-bulb temperature of **35°C**), predict — without recalculating — the direction of change for:
 - a) the approach temperature achievable;
 - b) the make-up water requirement;
 - c) the required air mass flow rate.
 Justify each answer qualitatively.

Exercise 2: (Graded out of 08 points)

Tomato juice at a feed flow rate of **5.5 kg/s** and inlet temperature of **60°C** is concentrated in a double-effect forward-feed evaporator. Live steam is supplied to the first effect at a pressure of **198.5 kPa** (abs).

The operating conditions and design parameters of each effect are given in the table below:

	First effect	Second effect
Heat transfer area, m²	100	100
Overall heat transfer coefficient, W/m².°C	2 000	1 000
Saturation pressure, kPa	90	17.9
Heat capacity at the exit, J/kg.°C	3 800	3 450

Additional data:

- Feed solids content = **11%** (mass basis),
- Feed heat capacity = **3900 J/kg.°C**,
- Assume no boiling point elevation,
- Condensate leaves each effect at the saturation temperature,
- Steady-state operation.

Required:

- 1) Determine the saturation temperature of live steam, and the boiling liquid in each effect,
- 2) Draw a clear schematic diagram of the multiple-effect evaporator used,
- 3) Determine the total solids flow rate in the system,
- 4) Determine the final mass flow rate of concentrated product,
- 5) Calculate the heat duty in the first effect,
- 6) Determine the amount of steam required,
- 7) Determine amount of vapour produced in the first effect,
- 8) Determine solids fraction of the liquid leaving the first effect,
- 9) Calculate the heat duty in the second effect,
- 10) Determine vapour produced in the second effect,
- 11) Determine final mass flow rate of product,
- 12) Determine final solids fraction,
- 13) Calculate steam economy.