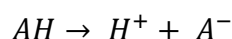
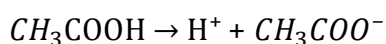
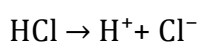


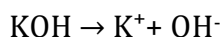
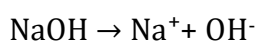
CHAPTER II. *Acids - Bases***1. Definitions of acids and bases****1.1. Acids and bases according to Arrhenius**

August Arrhenius first introduced the concept of acids and bases in the 1890s, According to Arrhenius.

An acid is a substance that, when dissolved in water, increases the concentration of hydrogen ions ( $H^+$ ) into the solution. This can be represented by the general equation:

**Example**

A **base** is a substance that, when dissolved in water, increases the concentration of hydroxide ions ( $OH^-$ ).

**Example****1.2. Acids and bases according to Bronsted-Lowry**

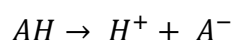
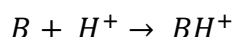
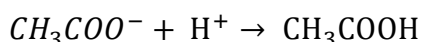
A more general definition of acids and bases was introduced by Johannes Bronsted and Thomas Lowry in the 1920s.

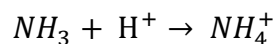
According to Bronsted-Lowry:

An acid is a chemical species that can donate a proton ( $H^+$ ), as represented by the following equation.

**Example**

A Base is a chemical species capable of capturing a proton ( $H^+$ ), as represented by the following equation:

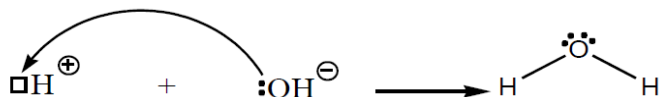
**Example**



### 1.3. Acids and Bases according to Lewis

An even broader (plus large) definition of acids and bases was proposed by Lewis in the 1920s, and his definitions are as follows :

- An acid is a compound that has a vacancy "Vacant cell": Electron acceptor.
- A base is a compound that has a free electron pair: Electron donor.



Lewis Acid

Lewis base

Electron Acceptor

Electron Donor

#### Example



### 2. Acid/Base couple in water

Every acid in solution has a corresponding conjugate base, and vice versa:

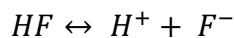


Where: **AH**. Acid

**A<sup>-</sup>** . Conjugate base

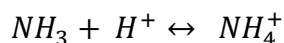
#### Example

Hydrofluoric acid HF:



The corresponding pair: (Acid/conjugate base) = (HF/F<sup>-</sup>)

Ammonia NH<sub>3</sub> (A base):



The corresponding pair: (Acid/conjugate base) = (NH<sub>4</sub><sup>+</sup>/NH<sub>3</sub>)

### 3. Acid-base reactions

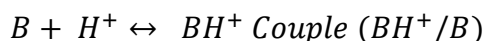
Protons (H<sup>+</sup>) do not exist in the free state. For an acid **AH** to be able to give up protons **H<sup>+</sup>**, it must have a base **B** capable of fixing them.

First half reaction :

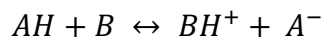
## CHAPTER II. Acids - Bases



Second half reaction:

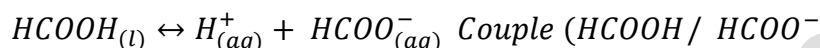


Acid-base reaction:

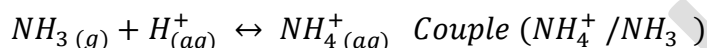


### Example

First half reaction :



Second half reaction:



Acid -base reaction:



### 4. Autodissociation of water

The autodissociation of water is the process by which two water molecules react with each other to produce a hydronium ion ( $H_3O^+$ ) and a hydroxide ion ( $OH^-$ ). This reaction is represented by the following equation :



A chemical equilibrium is then established between the water molecules, the hydronium ions and the hydroxide ions, called the water autoprotolysis equilibrium.

The equilibrium constant for this reaction is:

$$K = K_e = [H_3O^+] \times [OH^-]$$

Since no other ions can be present in pure water at 25 °C, the solution's electrical neutrality requires that:

$$[H_3O^+] = [OH^-] = 10^{-7}M$$

So,

$$K_e = [H_3O^+] \times [OH^-] = 10^{-14}$$

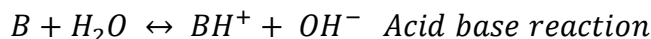
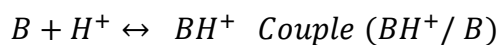
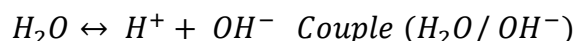
**Where:  $K_e$**  is the ionic product of water or autoprotolysis constant of water.

### 5. The Acid-Base role of water

Water can act as an acid or a base, so it has an amphoteric character (two roles).

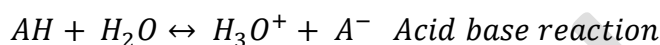
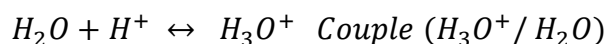
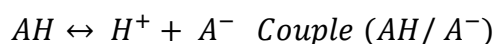
#### 5.1. As an acid

With a base B, water plays the role of an acid (Water can donate a proton ( $H^+$ ) to a base, forming a hydroxide ion ( $OH^-$ ).



## 5.2. As a base

With an acid AH, water plays the role of a base (Water can also accept a proton ( $H^+$ ) from an acid, forming a hydronium ion ( $H_3O^+$ ).



## 6. Strength of acids and bases

### 6.1. Acid strength

Consider the dissociation reaction of an acid, AH, in water:



$$K_e = \frac{[H_3O^+] \times [A^-]}{[AH]} = K_a$$

**With:**  $K_a$  is the acidity constant of the couple (AH/ $A^-$ )

Since the values of  $K_a$  are typically small (often negative powers of 10), it is preferred to use the base 10 logarithm of  $K_a$ , with the sign changed, a quantity known as  $pK_a$  :

$$pK_a = -\log_{10} K_a$$

### Note

An acid is considered stronger when its acidity constant  $K_a$  is higher (indicating a lower  $pK_a$ ). Conversely, an acid is weaker when its acidity constant  $K_a$  is lower (indicating a higher  $pK_a$ ).

### Example

Consider the two acid/base pairs:

$$pK_{a1}(CH_3COOH / CH_3COO^-) = 4.8$$

$$pK_{a2}(HCN / CN^-) = 9.2$$

The corresponding base constants are:

$$pK_{b1} 14 - 4.8 = 9.2$$

$$pK_{b2} 14 - 9.2 = 4.8$$

## CHAPTER II. Acids - Bases

Since:  $pK_{a1} < pK_{a2}$ , ( $CH_3COOH$ ) is a stronger acid than hydrogen cyanide ( $HCN$ ).

Since:  $pK_{b2} < pK_{b1}$ , ( $CN^-$ ) is a stronger base than ( $CH_3COO^-$ ).

Key take aways:

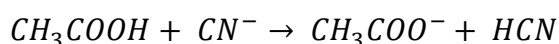
$K_a \uparrow \rightarrow pK_a \downarrow \rightarrow$  acid strength  $\uparrow$

$K_b \uparrow \rightarrow pK_b \downarrow \rightarrow$  base strength  $\uparrow$

A strong acid has a weak conjugate base, while a weak acid has a strong conjugate base.

In an acid–base reaction, the stronger acid donates a proton to the base.

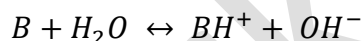
Therefore, acetic acid donates its proton to  $CN^-$ :



So, the reaction proceeds to the right, forming the weaker acid ( $HCN$ ) and the weaker base ( $CH_3COO^-$ ), which is thermodynamically favored.

### 6.2. Base strength

Consider the protonation reaction of a base B in the presence of water



$$K_b = \frac{[OH^-] \times [BH^+]}{[B]}$$

**With:**  $K_b$  is the basicity constant of the couple ( $BH^+/B$ )

$$pK_b = -\log_{10} K_b$$

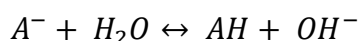
**Note:** A base is considered stronger when its basicity constant  $K_b$  is higher (indicating a lower  $pK_b$ ). Conversely, a base is weaker when its basicity constant  $K_b$  is lower (indicating a higher  $pK_b$ ).

### 6.3. Relationship between $K_a$ and $K_b$

Consider the pair ( $AH/A^-$ ):



$$K_a = \frac{[H_3O^+] \times [A^-]}{[AH]} \quad (1)$$



$$K_b = \frac{[OH^-] \times [AH]}{[A^-]} \quad (2)$$

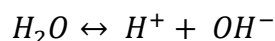
By multiplying equations (1) and (2), we obtain:

$$\begin{aligned} K_a \times K_b &= [H_3O^+][OH^-] = K_e = 10^{-14} \\ &\rightarrow pK_a + pK_b = pK_e = 14 \end{aligned}$$

### 6.4. The $pK_a$ of water pairs

Water can act as both an acid and a base, and it has two relevant  $pK_a$  values depending on which proton transfer equilibrium is considered.

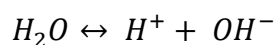
**1. Water acting as an acid:** When water donates a proton, it dissociates to form hydroxide ions ( $OH^-$ ):



The equilibrium constant for this dissociation is:

$$K_e = [H^+][OH^-] = 10^{-14} \rightarrow pK_a \approx 14$$

**2. Water acting as a base:** When water accepts a proton, it forms the hydronium ion ( $H_3O^+$ ):



For this protonation, the  $pK_a$  of the hydronium ion is approximately:

$$pK_a \approx -1.7$$

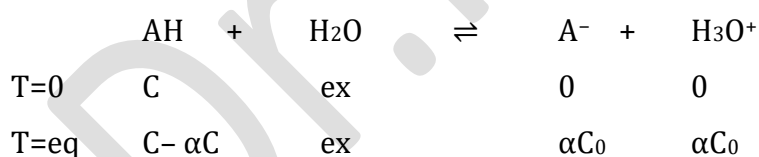
### 6.5. Ostwald's Dilution Law

Ostwald's dilution law is a fundamental principle in chemistry that deals with the dissociation of weak acids and bases in solution. It describes how the dilution of a solution affects the degree of dissociation of a weak acid or base.

As the concentration of a weak acid (or weak base) decreases, its tendency to dissociate increases, leading to a higher dissociation coefficient  $\alpha$ .

#### ✚ Weak acid

Consider the equilibrium of a weak acid HA



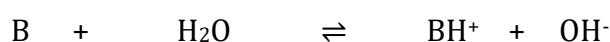
$$K_a = \frac{[A^-][H_3O^+]}{[AH]} = \frac{\alpha C \times \alpha C}{C(1-\alpha)} = \frac{\alpha^2}{(1-\alpha)} \rightarrow \frac{K_a}{C} = \frac{\alpha^2}{(1-\alpha)}$$

**Case 1:** If C increase => ( $K_a/C$ ) decrease => ( $\alpha^2 / (1-\alpha)$ ) decrease =>  $\alpha$  decrease

**Case 2:** If C decrease =>  $K_a/C$  increases => ( $\alpha^2 / (1-\alpha)$ ) increases =>  $\alpha$  increase.

#### ✚ Weak base

Consider the equilibrium of a weak base



## CHAPTER II. Acids - Bases

Give the dissociation coefficient ( $\alpha$ ) expressed in terms of  $K_b$  ?

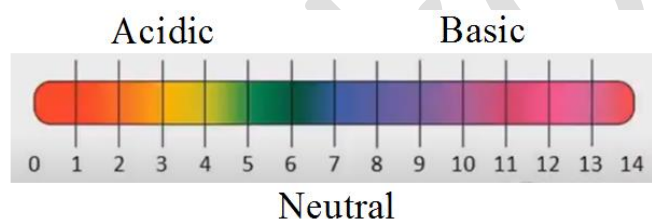
### 7. pH of Aqueous Solutions

The pH of an aqueous solution is a measure of its acidity or basicity, indicating the concentration of hydrogen ions ( $H^+$ ) present in the solution.

$$pH = -\log_{10}[H_3O^+]$$

The pH scale ranges from 0 to 14, with:

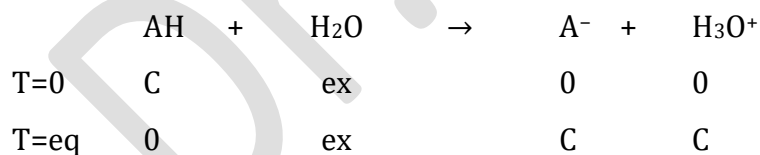
- ✚ **pH < 7** : Acidic solutions ( $[H_3O^+] > [OH^-]$ ).
- ✚ **pH = 7** : Neutral solutions ( $[H_3O^+] = [OH^-]$ ).
- ✚ **pH > 7** : Basic (or alkaline) solutions ( $[H_3O^+] < [OH^-]$ ).



#### 7.1. Case of a strong acid

If the acid AH is strong, it means it dissociates completely in water, and the equilibrium is fully shifted toward the products.

The reaction can be written as:



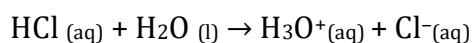
If  $[AH] = C \rightarrow [AH] = [H_3O^+] = C$

By definition  $\rightarrow pH = -\log_{10} [H_3O^+]$

$$\rightarrow pH = -\log_{10} C$$

#### Example

Calculate the pH of a 0.1 M solution of HCl.

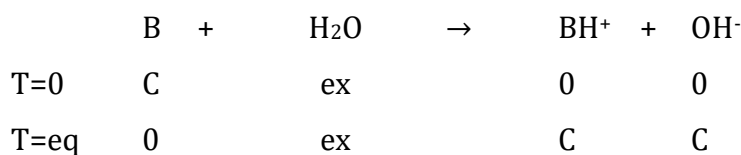


0.1 M                      0.1 M

$[H_3O^+] = C =$  The original concentration of the strong acid  $[HCl] = 0.1 M$

$$\text{pH} = -\log [\text{H}_3\text{O}^+] = -\log (0.1) = 1$$

### 7.2. Case of a strong base



Since B is a strong base, it dissociates completely in water:

$$\text{if } [\text{B}] = \text{C} \rightarrow [\text{B}] = [\text{OH}^-] = \text{C}$$

By definition  $\text{pOH} = -\log [\text{OH}^-]$

$$\text{And since: } \text{pH} + \text{pOH} = 14 \rightarrow \text{pH} = 14 - \text{pOH}$$

We have:

$$\rightarrow \text{pH} = 14 + \log_{10}[\text{H}_3\text{O}^+]$$

### Example

Let's take a solution of NaOH, a strong base, with a concentration of ( $C = 0.01 \text{ mol/L}$ ).

Since NaOH is a strong base, it dissociates completely in water:

$$\text{So: } [\text{NaOH}] = [\text{OH}^-] = C = 0.01 \text{ mol/L}$$

$$\text{pH} = 14 + \log_{10} [\text{H}_3\text{O}^+]$$

$$\text{pH} = 14 + \log_{10} (0.01) = 12$$

### 7.3. Case of a weak acid

A weak acid AH with concentration C in water, partially dissociates according to the following reaction:



#### 1. according to the law of conservation of mass

$$C = [\text{AH}] + [\text{A}^-] \text{ and } [\text{AH}] \gg [\text{A}^-], [\text{AH}] + [\text{A}^-] \approx [\text{AH}] \rightarrow C = [\text{AH}]$$

#### 2. according to the electroneutrality law

$$\sum \text{positive charges} = \sum \text{negative charges} \rightarrow [\text{H}_3\text{O}^+] = [\text{A}^-] + [\text{OH}^-]$$

## CHAPTER II. Acids - Bases

The medium is acidic  $[H_3O^+] \gg [OH^-] \rightarrow [H_3O^+] \gg [A^-] \rightarrow K_a = \frac{[A^-][H_3O^+]}{[AH]}$

$$\rightarrow K_a \cdot C = [H_3O^+]^2 \rightarrow [H_3O^+] = (K_a \cdot C)^{1/2} \rightarrow -\log_{10} [H_3O^+] = -\log_{10} (K_a \cdot C)^{1/2}$$

$$= \frac{1}{2} (-\log_{10} K_a - \log C) = \frac{1}{2} (pK_a - \log C)$$

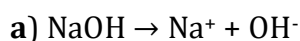
$$\rightarrow \mathbf{pH = \frac{1}{2} (pK_a - \log_{10} C)}$$

### Example

Calculate the pOH and pH of the following strong base solutions:

- 0.05 M NaOH,
- 0.05 M La(OH)<sub>3</sub>.

### Solution



$$0.05 \text{ M} \quad 0.05 \text{ M}$$

$$pOH = -\log [OH^-] = -\log (5 \times 10^{-2}) = 1.3$$

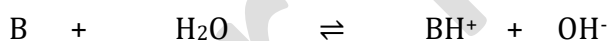
$$\text{As } pH + pOH = 14 \rightarrow pH = 14 - 1.3 = 12.7$$



$$pOH = 0.82 \rightarrow pH = 13.18$$

### 7.4. Case of a weak base

A weak base B with concentration C, in water, partially dissociates according to the following reaction:



The base dissociation constant  $K_b$  is given by :

$$K_b = \frac{[BH^+][OH^-]}{[B]}$$

#### 1. according to the law of conservation of mass

$$C = [B] + [BH^+] \text{ and } [B] \gg [BH^+], [B] + [BH^+] \approx [B] \rightarrow C = [B]$$

#### 2. according to the electroneutrality law

$$\sum \text{positive charges} = \sum \text{negative charges} \rightarrow [OH^-] = [BH^+] + [H_3O^+]$$

$$\text{The medium is basic } [OH^-] \gg [H_3O^+] \rightarrow [H_3O^+] = [BH^+] \rightarrow K_b = \frac{[BH^+][OH^-]}{[B]}$$

## CHAPTER II. Acids - Bases

$$\begin{aligned} \rightarrow K_b \cdot C &= [\text{OH}^-]^2 \rightarrow [\text{OH}^-] = (K_b \cdot C)^{1/2} \rightarrow -\log_{10} [\text{OH}^-] = -\log_{10} (K_b \cdot C)^{1/2} \\ &= \frac{1}{2} (-\log_{10} K_b - \log_{10} C) = \frac{1}{2} (\text{p}K_b - \log_{10} C) \end{aligned}$$

$$\rightarrow \text{pOH} = \frac{1}{2} (\text{p}K_b - \log_{10} C)$$

In an aqueous solution at 25°C, we have:

$$\text{pH} + \text{pOH} = 14 \text{ and } \text{p}K_a + \text{p}K_b = 14$$

From the equation:

$$14 - \text{pH} = \frac{1}{2}(14 - \text{p}K_a - \log_{10} C) = 7 - \frac{1}{2}(\text{p}K_a + \log_{10} C) \rightarrow \text{pH} = 14 - 7 + \frac{1}{2}(\text{p}K_a + \log_{10} C)$$

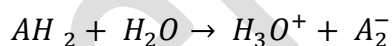
We find:

$$\rightarrow \text{pH} = 7 + \frac{1}{2} (\text{p}K_a + \log_{10} C)$$

### 8. pH of mixed solutions

#### 8.1. Case of a mixture of two strong acids (AH<sub>1</sub> and AH<sub>2</sub>)

When two strong acids are mixed, each one dissociates completely in water according to the reaction:



As both acids release hydronium ions (H<sub>3</sub>O<sup>+</sup>) into the solution, the total concentration of [H<sub>3</sub>O<sup>+</sup>] in the final mixture is the sum of the contributions from both acids.

If: C<sub>AH1</sub>: molar concentration of the first strong acid

C<sub>AH2</sub>: molar concentration of the second strong acid

Because both acids are completely dissociated

$$[\text{H}_3\text{O}^+] = C_{\text{AH1}} + C_{\text{AH2}}$$

By definition:

$$\rightarrow \text{pH} = -\log_{10} [\text{H}_3\text{O}^+] = -\log_{10} (C_{\text{AH1}} + C_{\text{AH2}})$$

#### Example

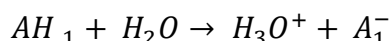
If we mix two strong acids: HCl at 0.01 M and HNO<sub>3</sub> at 0.02 M, the pH of the final solution

$$[\text{H}_3\text{O}^+] = C_{\text{AH1}} + C_{\text{AH2}} = 0.01 + 0.02 = 0.03$$

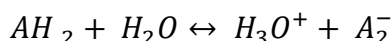
$$\text{So: } \text{pH} = -\log_{10} [\text{H}_3\text{O}^+] = -\log_{10} (0.03) \approx 1.52$$

### 8.2. Case of a mixture of a strong acid (AH<sub>1</sub>) and a weak acid (AH<sub>2</sub>).

Strong acid (AH<sub>1</sub>) : completely dissociates



Weak acid (AH<sub>2</sub>): partially dissociates



With equilibrium constant:

$$K_a = \frac{[H_3O^+][A_2^-]}{[AH_2]}$$

Because the strong acid (AH<sub>1</sub>) dissociates completely, it produce a large concentration of H<sub>3</sub>O<sup>+</sup>, this shifts the equilibrium of the weak acid to the left (Le Châtelier's principle), suppressing its dissociation even more.

As a result, the contribution of (AH<sub>2</sub>) to ([H<sub>3</sub>O<sup>+</sup>]) is negligible compared to that of (AH<sub>1</sub>).

So the total hydronium concentration

$$[H_3O^+] = [H_3O^+] (\text{from } AH_1) + [H_3O^+] (\text{from } AH_2)$$

Since: [H<sub>3</sub>O<sup>+</sup>] (from AH<sub>2</sub>) is very small

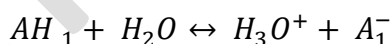
So: [H<sub>3</sub>O<sup>+</sup>] = [H<sub>3</sub>O<sup>+</sup>] (from AH<sub>1</sub>) = C<sub>AH<sub>1</sub></sub>

By definition:

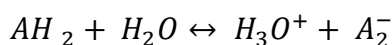
$$\rightarrow pH = -\log_{10}[H_3O^+] = -\log_{10}(C_{AH1})$$

### 8.3. Case of a mixture of two weak acids (AH<sub>1</sub>) and (AH<sub>2</sub>).

Weak acid (AH<sub>1</sub>) : partially dissociates



Weak acid (AH<sub>2</sub>): partially dissociates



Their acid dissociation constant are:

$$K_{a,AH_1} = \frac{[H_3O^+][A_1^-]}{[AH_1]}$$

$$K_{a,AH_2} = \frac{[H_3O^+][A_2^-]}{[AH_2]}$$

Since both acids are weak

$$x = [H_3O^+]$$

Since both acids are weak ( $x \ll [H_3O^+]$ ), we can approximate:

$$[AH_1] \approx C_{AH1}, [AH_2] \approx C_{AH2}$$

From the equilibrium constants

$$K_{a,AH_1} = \frac{[H_3O^+][A_1^-]}{[AH_1]} \rightarrow [A_1^-] = \frac{K_{a,AH_1} \times C_{AH_1}}{x}$$

$$K_{a,AH_2} = \frac{[H_3O^+][A_2^-]}{[AH_2]} \rightarrow [A_2^-] = \frac{K_{a,AH_2} \times C_{AH_2}}{x}$$

$$x = \frac{K_{a,AH_1} \times C_{AH_1}}{x} + \frac{K_{a,AH_2} \times C_{AH_2}}{x}$$

$$x^2 = K_{a,AH_1} \times C_{AH_1} + K_{a,AH_2} \times C_{AH_2}$$

$$[H_3O^+] = \sqrt{K_{a,AH_1} \times C_{AH_1} + K_{a,AH_2} \times C_{AH_2}}$$

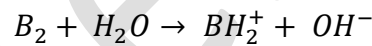
By definition

$$pH = -\log_{10}[H_3O^+]$$

$$\rightarrow pH = -\frac{1}{2} \log(K_{a(AH_1)} \cdot C_{AH_1} + K_{a(AH_2)} \cdot C_{AH_2})$$

#### 8.4. Case of a mixture of two strong bases

Each strong base dissociates completely in water



Since both bases are strong, they fully dissociate, releasing hydroxide ( $OH^-$ ) ions into the solution.

Let:  $C_{B_1}$ : molar concentration of the first strong base

$C_{B_2}$ : molar concentration of the second strong base

Because dissociation is complete:

$$[OH^-]_{B_1} = C_{B_1}, [OH^-]_{B_2} = C_{B_2} \rightarrow [OH^-]_{TOT} = C_{B_1} + C_{B_2}$$

$$pOH = -\log_{10}[OH^-]$$

$$pOH = -\log_{10}(C_{B_1} + C_{B_2})$$

At 25°C, the relation is

$$pH + pOH = 14$$

Therefore:

$$pH = 14 - pOH$$

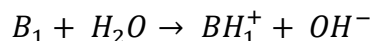
$$\text{Substitute } pOH = -\log_{10}(C_{B_1} + C_{B_2})$$

$$pH = 14 - (-\log_{10}(C_{B_1} + C_{B_2}))$$

$$\rightarrow pH = 14 + \log(C_{B_1} + C_{B_2})$$

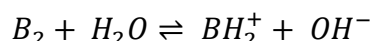
### 8.5. Case of a mixture of strong base on the weak base

Since  $B_1$  is a strong base, it dissociates completely in water:



Thus:  $[OH^-]_{B_1} = C_{B_1}$

Since  $B_2$  is a weak base, it dissociates partially according to



With:

$$K_b = \frac{[BH_2^+] \times [OH^-]}{[B_2]}$$

Since the strong base completely dissociates, it produces a large concentration of hydroxide ions ( $OH^-$ ), this increases the  $[OH^-]$  in the solution and therefore suppresses the dissociation of the weak base (Châtelier's principle).

Hence, the contribution of the weak base  $B_2$  to  $OH^-$  is negligible compared to that of the strong base  $B_1$ .

Total hydroxide concentration

$$[OH^-]_{TOT} = [OH^-]_{B_1} + [OH^-]_{B_2} \approx [OH^-]_{B_1}$$

Thus:  $[OH^-] = C_{B_1}$

$$pOH = -\log_{10}[OH^-] = -\log_{10}(C_{B_1})$$

And using the relation

$$pH + pOH = 14$$

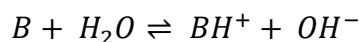
We obtain:

$$pH = 14 - pOH = 14 - (-\log_{10}(C_{B_1}))$$

$$\rightarrow pH = 14 + \log(C_{B_1})$$

### 8.5. Case of a mixture of two weak bases ( $B_1$ ) and ( $B_2$ )

**For a single weak base B:**



$$\text{With: } K_b = \frac{[BH^+] \times [OH^-]}{[B]}$$

At typical dilute conditions  $[B] \approx C_B$  and  $[OH^-] \ll C_B$  giving  $[OH^-] \approx \sqrt{K_b \cdot C_B}$

For the two weak bases in the same solution, their hydroxide contributions add:

$$[OH^-] \approx \sqrt{K_{b1} \cdot C_{B1} + K_{b2} \cdot C_{B2}}$$

$$K_{b1} \cdot K_{B2} = K_W$$

We have at 25°C:

$$pOH = -\log_{10}[OH^-] \text{ and } pH + pOH = 14$$

$$\text{So: } pH = 14 - \left(-\frac{1}{2} \log_{10}(K_{b1} \cdot C_{B1} + K_{b2} \cdot C_{B2})\right) = 14 + \frac{1}{2} \log_{10}(K_{b1} \cdot C_{B1} + K_{b2} \cdot C_{B2})$$

Because  $K_{b1} \cdot K_{B2} = K_W$  and  $K_W = 10^{-14}$  at 25°C we have  $K_b = \frac{K_w}{K_a}$

$$\text{Substitute: } K_{b1} \cdot C_{B1} + K_{b2} \cdot C_{B2} = K_w \left( \frac{C_{B1}}{K_{a,B1}} + \frac{C_{B2}}{K_{a,B2}} \right)$$

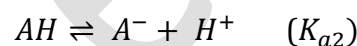
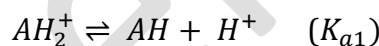
$$\text{Then: } pH = 14 + \frac{1}{2} \log K_w + \frac{1}{2} \log \left( \frac{C_{B1}}{K_{a,B1}} + \frac{C_{B2}}{K_{a,B2}} \right)$$

$$\text{Since: } \log K_w = \log 10^{-14} = -14$$

$$\rightarrow pH = 7 + \frac{1}{2} \log \left( \frac{C_{B1}}{K_{a,B1}} + \frac{C_{B2}}{K_{a,B2}} \right)$$

### 8.5. Case of an amphoteric solution

An amphoteric (amphiprotic) substance can act both as an acid or a base; it can donate or accept a proton; leading to two equilibria:



At equilibrium, for the amphoteric species AH, we have two acid dissociation constants:

$$K_{a1} = \frac{[H^+][AH]}{[AH_2^+]}$$

$$K_{a2} = \frac{[H^+][A^-]}{[AH]}$$

At the isoelectric point (where the species mainly exists as AH), the concentration of  $[AH_2^+]$  and  $[A^-]$  are approximately equal:  $[AH_2^+] = [A^-]$

So by multiplying both equations:

$$K_{a1} \cdot K_{a2} = \frac{[H^+][AH]}{[AH_2^+]} \cdot \frac{[H^+][A^-]}{[AH]} = [H^+]^2 \frac{[A^-]}{[AH_2^+]}$$

But since  $[AH_2^+] = [A^-]$

$$\text{So } K_{a1} \cdot K_{a2} = [H^+]^2$$

$$[H]^+ = \sqrt{K_{a1} \cdot K_{a2}}$$

$$pH = -\log_{10}[H^+] = -\frac{1}{2} \log(K_{a1} \cdot K_{a2})$$

$$\rightarrow pH = \frac{1}{2} \log(pK_{a_1} + pK_{a_2})$$

### 8.6. Case of salts solution

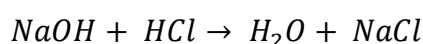
When a salt dissolves in water, it dissociates into its ions.

Depending on whether those ions come from strong or weak acids/bases, they may or may not react (hydrolyze) with water, which affects the pH.

#### a. Salt of a strong acid and a strong base

##### Example

NaCl (from NaOH and HCl):



The resulting salt (NaCl) dissociates completely into (Na<sup>+</sup>) and (Cl<sup>-</sup>) ions, which are neutral and do not react with water.



Since there is no excess acid or base, and the ions from the salt do not affect water equilibrium:

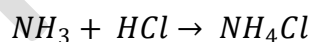
$$[H_3O^+] = [OH^-]$$

$$\rightarrow pH = 7$$

#### b. Salt of a strong acid and a weak base

##### Example

NH<sub>4</sub>Cl (from NH<sub>3</sub> and HCl)



In water, NH<sub>4</sub>Cl dissociate completely



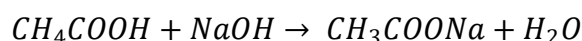
Since, the conjugate base of the strong acid is a base of zero strength, and the conjugate acid of the weak base is a weak acid, the pH of the solution is that of weak acid:

$$\rightarrow pH = \frac{1}{2} (pK_a - \log C_{salts})$$

#### c. Salt of a weak acid and a strong base

##### Example

CH<sub>3</sub>COONa (from CH<sub>3</sub>COOH and NaOH)



In aqueous solution, sodium acetate dissociates completely



Since, Na<sup>+</sup> is the cation of a strong base it does not hydrolyse, while the CH<sub>3</sub>COO<sup>-</sup> the conjugate base of the weak acid (CH<sub>3</sub>COOH) undergoes hydrolysis, so the pH of the solution is:

$$\rightarrow pH = 7 + \frac{1}{2} (pK_a - \log C_{salts})$$

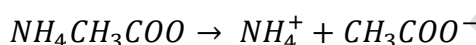
#### d. Salt of a weak acid and a weak base

##### Example

NH<sub>4</sub>CH<sub>3</sub>COO (from NH<sub>3</sub> and CH<sub>3</sub>COOH):



In water, ammonium acetate dissociates completely



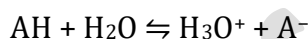
Both ions can hydrolyze in water, so, both hydrolysis reactions occur simultaneously, so the pH of the solution is:

Both ions can hydrolyze in water; therefore, the two hydrolysis reactions occur simultaneously, and the pH of the solution depends on the relative strengths of the conjugate acid and the conjugate base.

$$\rightarrow pH = \frac{1}{2} (pK_a + pK_b)$$

#### 8.7. Case of buffer solution

A buffer solution is composed of a mixture of a weak acid AH and its conjugate base A<sup>-</sup>. The equilibrium for this system can be represented as follows:



The acid dissociation constant K<sub>a</sub> for the acid-base pair AH/A<sup>-</sup> is defined by the equation

$$K_a = \frac{[A^-][H_3O^+]}{[AH]}$$

$$-\log K_a = -\log \left( \frac{[A^-][H_3O^+]}{[AH]} \right)$$

$$-\log K_a = -\log([H_3O^+]) - \log \left( \frac{[A^-]}{[AH]} \right)$$

$$-\log([H_3O^+]) = -\log K_a + \log \left( \frac{[A^-]}{[AH]} \right)$$

$$\rightarrow pH = pK_a + \log_{10} \left( \frac{[A^-]}{[AH]} \right) = pK_a + \log_{10} \left( \frac{[Base]}{[Acid]} \right)$$

The buffer zone  $pK_a - 1 < pH < pK_a + 1$

### 9. Color indicators

A color indicator is typically a weak monoprotic acid with a specific pKa, where the form HA has a distinctly different color from its conjugate base form A<sup>-</sup>.

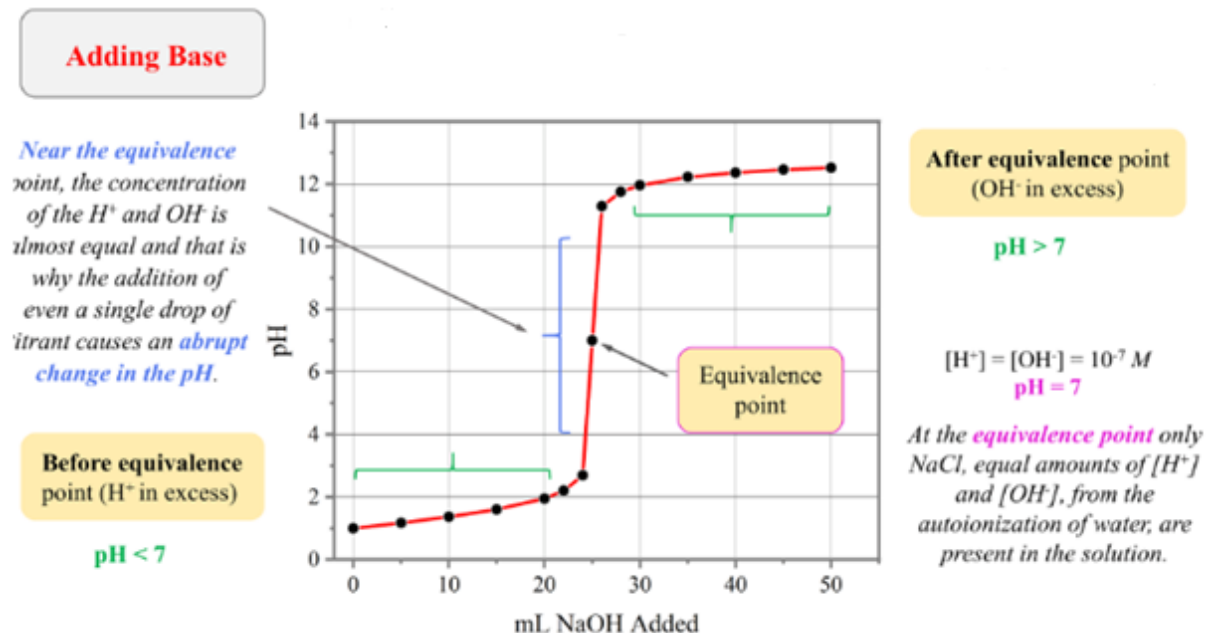
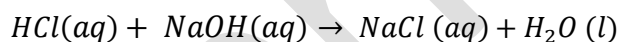
**Table 1.** Some indicators and their color change range

Indicator	Color change range	Color in acidic state	Color in basic state
Thymol Blue	1.2 - 2.8	Red	Yellow
Methyl Orange	3.1 - 4.4	Orange	Yellow
Phenol Red	6.6 - 8.0	Yellow	Red
Bromothymol Blue	6.0 - 7.6	Yellow	Blue
Phenolphthalein	8.3 - 10	Colorless	Pink

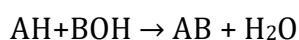
### 10. Acid-Base titrations

#### 10.1. Titration of a strong acid by a strong base

##### Example



The strong acid and strong base dissociate completely in water.



The titration curve can be divided into three distinct parts:

#### Before the equivalence point

## CHAPTER II. Acids - Bases

Before the equivalence point,  $C_a \cdot V_a$  is greater than  $C_b \cdot V_b$  ( $[H_3O^+] > [OH^-]$ ). The  $OH^-$  ions react with an equal number of  $H_3O^+$  ions to form water, leaving in solution a remaining amount of  $H_3O^+$  ions equal to  $C_a \cdot V_a - C_b \cdot V_b$ .

$$[H_3O^+] = \frac{C_a V_a - C_b V_b}{V_a + V_b}$$

$$pH = -\log_{10} \left( \frac{C_a V_a - C_b V_b}{V_a + V_b} \right)$$

### At the equivalence point

This corresponds to calculating the pH of a strong acid solution that has been exactly neutralized by a strong base :

$C_a \cdot V_a = C_b \cdot V_b$  ( $[H_3O^+] = [OH^-]$ ). At this point,  $pH=7$  at  $25^\circ C$ .

### After the equivalence point

After the equivalence point,  $C_a \cdot V_a$  is less than  $C_b \cdot V_b$  ( $[OH^-] > [H_3O^+]$ ). The  $OH^-$  ions react with all the  $H_3O^+$  ions to form water, leaving in solution an amount of  $OH^-$  ions equal to  $C_b \cdot V_b - C_a \cdot V_a$ .

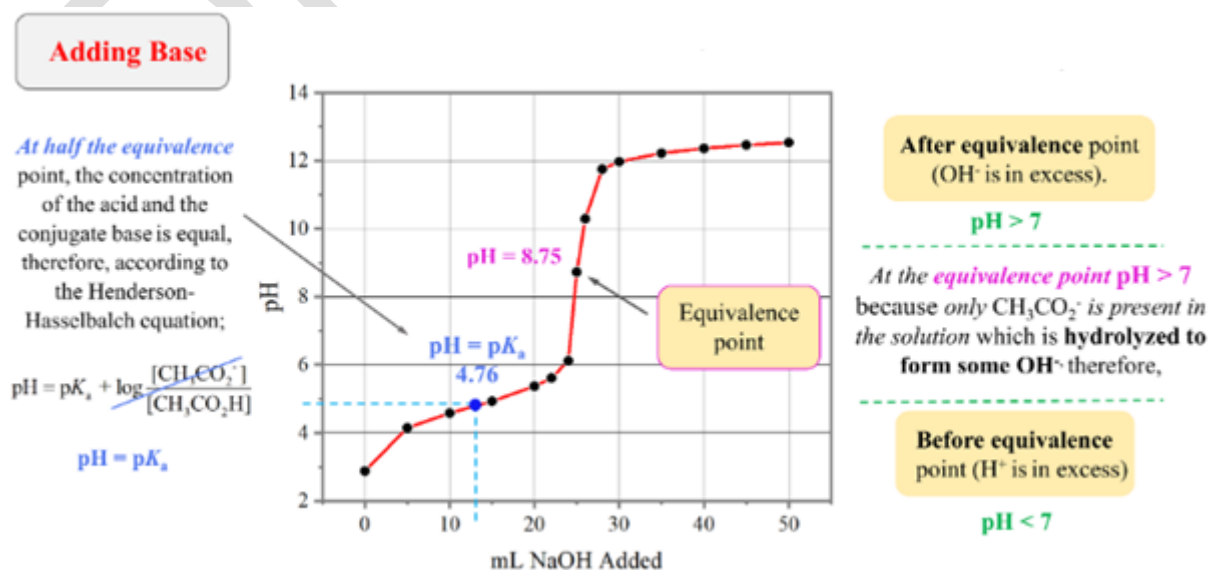
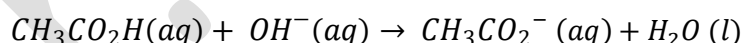
$$[OH^-] = \frac{C_b V_b - C_a V_a}{V_a + V_b}$$

$$pOH = -\log_{10} \left( \frac{C_b V_b - C_a V_a}{V_a + V_b} \right)$$

$$pH = 14 + \log_{10} \left( \frac{C_b V_b - C_a V_a}{V_a + V_b} \right)$$

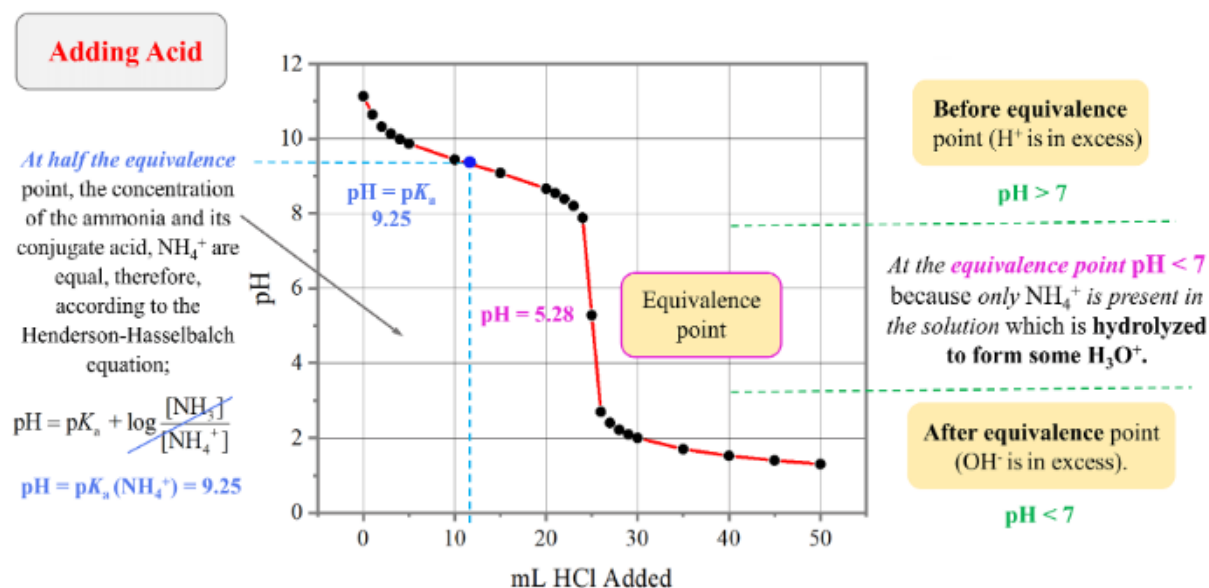
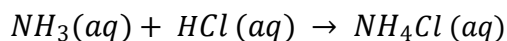
## 9.2. Titration of a weak acid by a strong base

### Example



### 9.3. Titration of a strong acid with a weak base

#### Example



### 9.4. Titration of a polyacid with a strong base

