

## Tutorial 1: Thermodynamics of solutions

### Exercise 1

For a binary mixture, prove that the partial molar property of constituent 2 is written as follows:

$$\bar{M}_2 = M_m + (1 - x_2) \left( \frac{\partial M_m}{\partial x_2} \right)_{P,T,n_1} \quad \text{and} \quad \bar{M}_1 = M_m - x_1 \left( \frac{\partial M_m}{\partial x_1} \right)_{P,T,n_1}$$

### Exercise 2

The volume of a binary mixture has a molar volume,  $V$ , that depends on its composition given by the following expression:

$$V_m = 75x_1 + 95x_2 + 3.7x_1x_2 \left( \frac{\text{cm}^3}{\text{mol}} \right)$$

1. What is the pure species molar volume for component 1 and component 2.
2. For a mixture with  $x_1 = 0.60$ .

Determine:

- a) the molar volume of the mixture, and b) the partial molar volume of component 1.

### Exercise 3

The molar enthalpy of a binary liquid system of species 1 and 2 at fixed  $T$  and  $P$  is represented by the following equation:

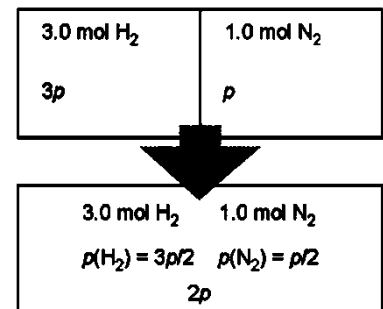
$$H = 400x_1 + 600x_2 + x_1x_2(40x_1 + 20x_2)$$

where  $H$  is in J/mol

- a. determine expressions for  $\bar{H}_1$  and  $\bar{H}_2$  as functions of  $x_1$
- b. Numerical values for the pure species enthalpies  $H_1^*$  and  $H_2^*$
- c. Find the expression of  $(H^E)$
- d. Numerical values for the partial enthalpies at infinite dilution  $\bar{H}_1$  and  $\bar{H}_2$

### Exercise 4

A container is divided into two equal compartments (figure below). One contains 3.0 mol of  $H_2$  at  $25^\circ\text{C}$ ; the other contains 1.0 mol  $N_2$  at  $25^\circ\text{C}$ . Calculate the *Gibbs energy of mixing* when the partition is removed. Assume perfect gas behavior.  $P^0 = 1\text{bar}$



### Exercise 5

For a mixture contains 75%  $H_2$  and 25%  $N_2$  (molar basis) estimate the pseudo critical Temperature and pressure ( $P_{pc}$  and  $T_{pc}$ ) using Kay's rule.

We give:

For  $N_2$ :  $T_C = 126.2\text{K}$  and  $P_C = 33.5\text{atm}$

For  $H_2$   $T_C = 33 + 8 = 41K$  and  $P_C = 12.8 + 8 = 20.8 atm$

### Exercise 6

Determine the specific volume  $v$  ( $m^3/kg$ ) of a **methane-ethane gas mixture** at **16 MPa and 250°C**, where the mixture contains: 60 mol% **methane (CH<sub>4</sub>)** and 40 mol% **ethane (C<sub>2</sub>H<sub>6</sub>)**

- Assume the mixture ideal (with the mixture gas constant).
- Consider a real mixture (the generalized compressibility chart).
- determine which method provides the more accurate result and explain why.

Given:  $M_{CH_4} = 16.04 g/mol$ ,  $M_{C_2H_6} = 30.07 g/mol$

Table: Molar mass gas constant and critical point properties-point properties

Chart: Compressibility factor  $Z$  as function of  $P_{pc}$

TABLE A-1

Molar mass, gas constant, and critical-point properties

| Substance                      | Formula                           | Molar mass,<br>$M$ kg/kmol | Gas<br>constant,<br>$R$ kJ/kg·K* | Critical-point properties |                  |                       |
|--------------------------------|-----------------------------------|----------------------------|----------------------------------|---------------------------|------------------|-----------------------|
|                                |                                   |                            |                                  | Temperature,<br>K         | Pressure,<br>MPa | Volume,<br>$m^3/kmol$ |
| Air                            | —                                 | 28.97                      | 0.2870                           | 132.5                     | 3.77             | 0.0883                |
| Ammonia                        | NH <sub>3</sub>                   | 17.03                      | 0.4882                           | 405.5                     | 11.28            | 0.0724                |
| Argon                          | Ar                                | 39.948                     | 0.2081                           | 151                       | 4.86             | 0.0749                |
| Benzene                        | C <sub>6</sub> H <sub>6</sub>     | 78.115                     | 0.1064                           | 562                       | 4.92             | 0.2603                |
| Bromine                        | Br <sub>2</sub>                   | 159.808                    | 0.0520                           | 584                       | 10.34            | 0.1355                |
| <i>n</i> -Butane               | C <sub>4</sub> H <sub>10</sub>    | 58.124                     | 0.1430                           | 425.2                     | 3.80             | 0.2547                |
| Carbon dioxide                 | CO <sub>2</sub>                   | 44.01                      | 0.1889                           | 304.2                     | 7.39             | 0.0943                |
| Carbon monoxide                | CO                                | 28.011                     | 0.2968                           | 133                       | 3.50             | 0.0930                |
| Carbon tetrachloride           | CCl <sub>4</sub>                  | 153.82                     | 0.05405                          | 556.4                     | 4.56             | 0.2759                |
| Chlorine                       | Cl <sub>2</sub>                   | 70.906                     | 0.1173                           | 417                       | 7.71             | 0.1242                |
| Chloroform                     | CHCl <sub>3</sub>                 | 119.38                     | 0.06964                          | 536.6                     | 5.47             | 0.2403                |
| Dichlorodifluoromethane (R-12) | CCl <sub>2</sub> F <sub>2</sub>   | 120.91                     | 0.06876                          | 384.7                     | 4.01             | 0.2179                |
| Dichlorofluoromethane (R-21)   | CHCl <sub>2</sub> F               | 102.92                     | 0.08078                          | 451.7                     | 5.17             | 0.1973                |
| Ethane                         | C <sub>2</sub> H <sub>6</sub>     | 30.070                     | 0.2765                           | 305.5                     | 4.48             | 0.1480                |
| Ethyl alcohol                  | C <sub>2</sub> H <sub>5</sub> OH  | 46.07                      | 0.1805                           | 516                       | 6.38             | 0.1673                |
| Ethylene                       | C <sub>2</sub> H <sub>4</sub>     | 28.054                     | 0.2964                           | 282.4                     | 5.12             | 0.1242                |
| Helium                         | He                                | 4.003                      | 2.0769                           | 5.3                       | 0.23             | 0.0578                |
| <i>n</i> -Hexane               | C <sub>6</sub> H <sub>14</sub>    | 86.179                     | 0.09647                          | 507.9                     | 3.03             | 0.3677                |
| Hydrogen (normal)              | H <sub>2</sub>                    | 2.016                      | 4.1240                           | 33.3                      | 1.30             | 0.0649                |
| Krypton                        | Kr                                | 83.80                      | 0.09921                          | 209.4                     | 5.50             | 0.0924                |
| Methane                        | CH <sub>4</sub>                   | 16.043                     | 0.5182                           | 191.1                     | 4.64             | 0.0993                |
| Methyl alcohol                 | CH <sub>3</sub> OH                | 32.042                     | 0.2595                           | 513.2                     | 7.95             | 0.1180                |
| Methyl chloride                | CH <sub>3</sub> Cl                | 50.488                     | 0.1647                           | 416.3                     | 6.68             | 0.1430                |
| Neon                           | Ne                                | 20.183                     | 0.4119                           | 44.5                      | 2.73             | 0.0417                |
| Nitrogen                       | N <sub>2</sub>                    | 28.013                     | 0.2968                           | 126.2                     | 3.39             | 0.0899                |
| Nitrous oxide                  | N <sub>2</sub> O                  | 44.013                     | 0.1889                           | 309.7                     | 7.27             | 0.0961                |
| Oxygen                         | O <sub>2</sub>                    | 31.999                     | 0.2598                           | 154.8                     | 5.08             | 0.0780                |
| Propane                        | C <sub>3</sub> H <sub>8</sub>     | 44.097                     | 0.1885                           | 370                       | 4.26             | 0.1998                |
| Propylene                      | C <sub>3</sub> H <sub>6</sub>     | 42.081                     | 0.1976                           | 365                       | 4.62             | 0.1810                |
| Sulfur dioxide                 | SO <sub>2</sub>                   | 64.063                     | 0.1298                           | 430.7                     | 7.88             | 0.1217                |
| Tetrafluoroethane (R-134a)     | CF <sub>3</sub> CH <sub>2</sub> F | 102.03                     | 0.08149                          | 374.2                     | 4.059            | 0.1993                |
| Trichlorofluoromethane (R-11)  | CCl <sub>3</sub> F                | 137.37                     | 0.06052                          | 471.2                     | 4.38             | 0.2478                |
| Water                          | H <sub>2</sub> O                  | 18.015                     | 0.4615                           | 647.1                     | 22.06            | 0.0560                |
| Xenon                          | Xe                                | 131.30                     | 0.06332                          | 289.8                     | 5.88             | 0.1186                |

\*The unit kJ/kg·K is equivalent to kPa·m<sup>3</sup>/kg·K. The gas constant is calculated from  $R = R_u/M$ , where  $R_u = 8.31447$  kJ/kmol·K and  $M$  is the molar mass.

Source: K. A. Kobe and R. E. Lynn, Jr., *Chemical Review* 52 (1953), pp. 117–236; and ASHRAE, *Handbook of Fundamentals* (Atlanta, GA: American Society of Heating, Refrigerating and Air-Conditioning Engineers, Inc., 1993), pp. 16.4 and 36.1.

# Compressibility Factors for Natural Gases as a Function of Pseudoreduced Pressure and Temperature.

